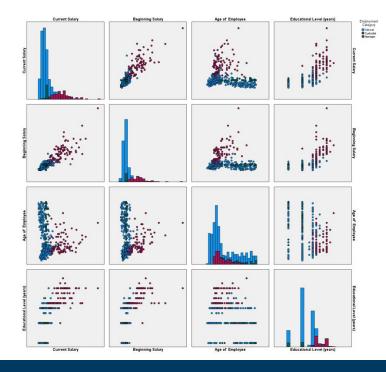


Correlation analysis with SPSS Statistics

Jarlath Quinn – Analytics Consultant





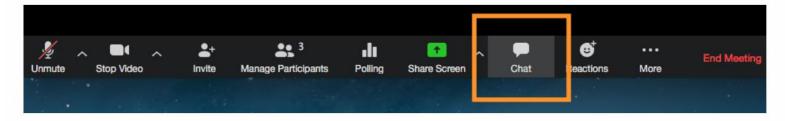
Correlation analysis with SPSS Statistics

Just waiting for all attendees to join...

Jarlath Quinn – Analytics Consultant

FAQ's

- Is this session being recorded? Yes
- Can I get a copy of the slides? Yes, we'll email links to download materials after the session has ended.
- Can we arrange a re-run for colleagues? Yes, just ask us.
- How can I ask questions? All lines are muted so please use the chat panel if we run out of time we will follow up with you.











- Gold accredited partner to IBM, Predictive Solutions and DataRobot specialising in advanced analytics & big data technologies
- Work with open source technologies (R, Python, Spark etc.)
- Team each has 15 to 30 years of experience working in the advanced and predictive analytics industry

- Deep experience of applied advanced analytics applications across sectors
 - Retail
 - Gaming
 - Utilities
 - Insurance
 - Telecommunications
 - Media
 - FMCG



Agenda

- Why are correlation values useful?
- Interpreting correlation coefficients
- Estimating correlation values with bootstrapping techniques
- Automatically highlighting strong correlations
- How correlations are calculated
- Non-parametric correlations
- The limitations of correlations





Correlations

| | | Current Salary |
|---------------------------|---------------------|----------------|
| Educational Level (years) | Pearson Correlation | .661** |
| | Sig. (2-tailed) | <.001 |
| | N | 474 |

^{**.} Correlation is significant at the 0.01 level (2-tailed).

Why are correlations useful?

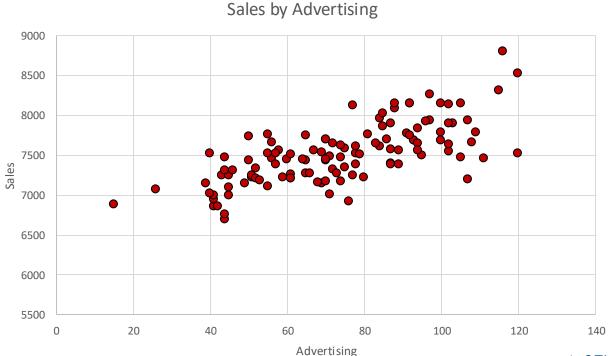
Why use correlations?

- Correlation is a term that we employ in everyday speech to denote things that appear to have some kind of relationship
- In analytics, correlations are specific values that are calculated in order quantify the relationships between variables
- This kind of analysis is powerful because, it allows us to <u>detect</u> and <u>measure</u> the strength of linear associations between an near infinite range of factors, such as:
 - Advertising spend and website hits
 - Product sales and competitor pricing
 - Vibration and component part failure
 - Rainfall and pollution
 - Study time and examination grade
 - Exercise and weight loss
 - Government spending and population health outcomes



The gateway to prediction

- Not only can we measure a linear relationship with correlation, but we can also use one variable to predict the other
- For example, if we know how much we're planning to increase our spend on advertising then we can use correlation to accurately predict what the increase in visitors to the website is likely to be.







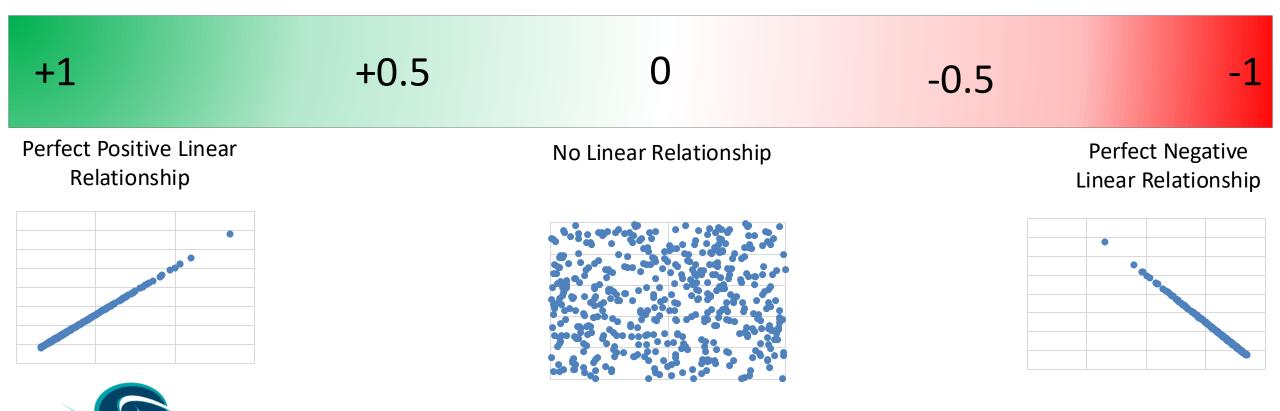
Correlations

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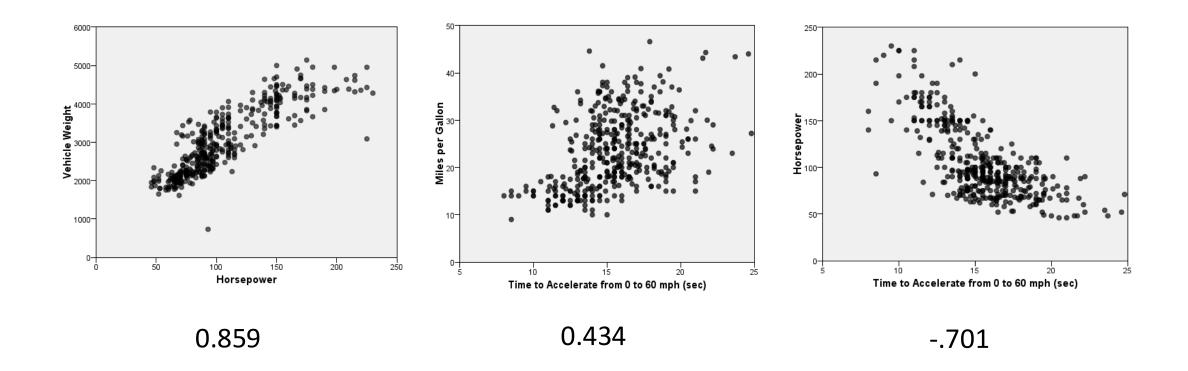
Interpreting correlations

Linear Correlation Scale



A SELECT INTERNATIONAL COMPANY

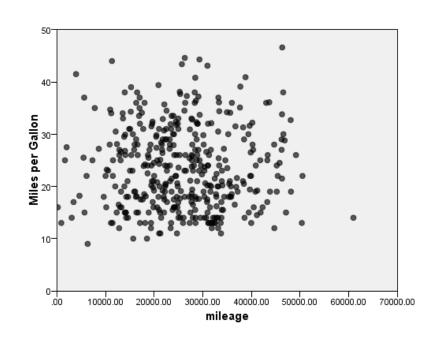
Pearson's r correlations

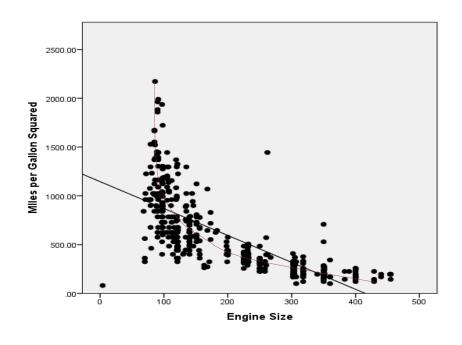




Pearson's *r* correlation coefficients

Non-Linear Relationships



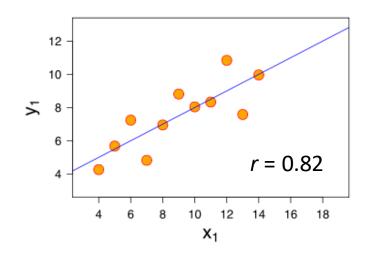


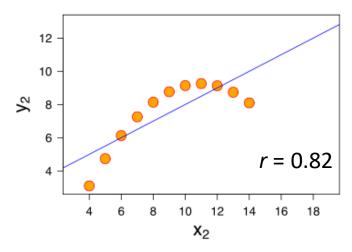
-0.005 -.671

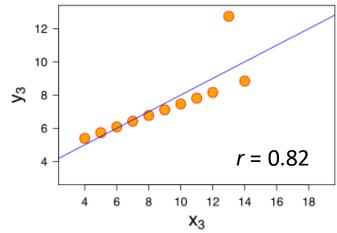


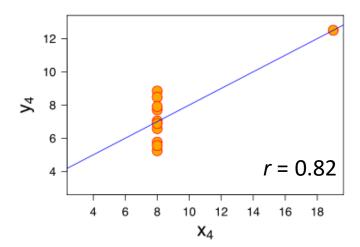
Pearson's *r* Correlations

A word of warning: always investigate the relationship





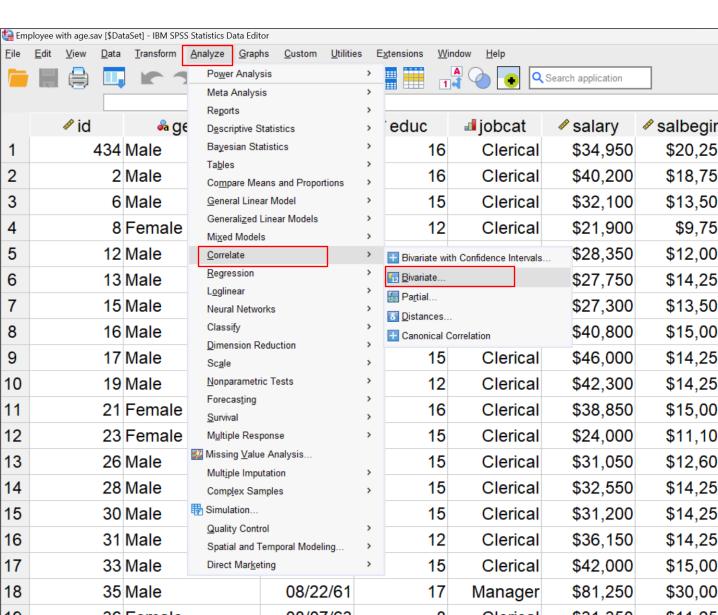




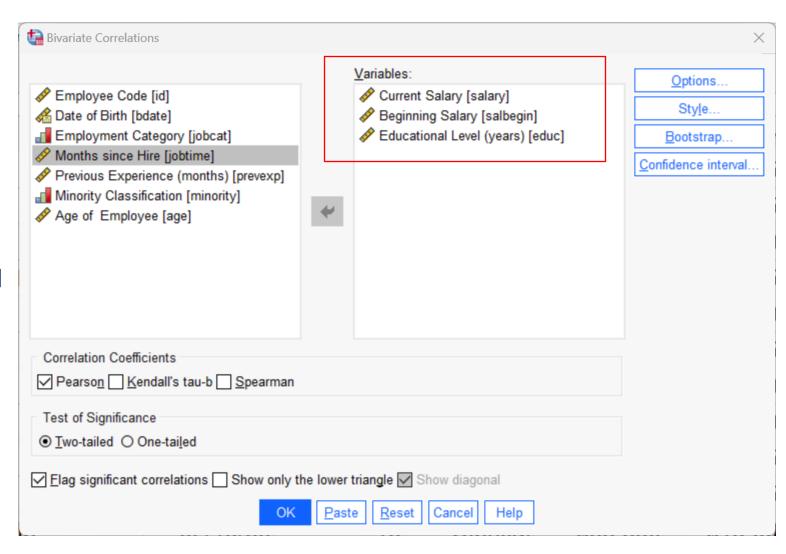


- Analyze
 - Correlate
 - Bivariate





- Three variables chosen so three pairs of correlations
 - 1. Current Salary x Beginning Salary
 - 2. Current Salary x Education Level
 - 3. Beginning Salary x Education Level





Correlations

| | | Current Salary | Beginning Salary | Educational Level (years) |
|---------------------------|---------------------|----------------|---------------------|------------------------------|
| Current Salary | Pearson Correlation | 1 | .880** | .661** |
| | Sig. (2-tailed) | | <.001 | <.001 |
| | N | 474 | 474 | 474 |
| Beginning Salary | Pearson Correlation | .880** | 1 | .633** |
| | Sig. (2-tailed) | <.001 | | <.001 |
| | N | 474 | 474 | 474 |
| Educational Level (years) | Pearson Correlation | .661** | .633** | 1 |
| | Sig. (2-tailed) | <.001 | <.001 | |
| | N | 474 | 474 | 474 |

^{**.} Correlation is significant at the 0.01 level (2-tailed).



Correlations

The table is a mirror image

| | | Current Salary | Beginning Salary | Educational Level (years) | |
|---------------------------|---------------------|----------------|---------------------|------------------------------|--|
| Current Salary | Pearson Correlation | 1 | .880** | .661** | |
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| | Sig. (2-tailed) | <.001 | <.001 | | |
| | N | 474 | 474 | 474 | |

^{**.} Correlation is significant at the 0.01 level (2-tailed).



The diagonal values are all equal to one as they are the variables correlated against themselves

Correlations

| | | Current Salary | Beginning Salary | Educational Level (years) |
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| | Sig. (2-tailed) | <.001 | <.001 | |
| | N | 474 | 474 | 474 |

^{**.} Correlation is significant at the 0.01 level (2-tailed).



Correlations

The Significance values show how likely one is to get a correlation like that assuming there's no relationship between the variables

| | | Current Salary | Beginning Salary | Educational Level (years) |
|---------------------------|---------------------|----------------|---------------------|------------------------------|
| Current Salary | Pearson Correlation | 1 | .880** | .661** |
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| | N | 474 | 474 | 474 |

^{**.} Correlation is significant at the 0.01 level (2-tailed).



Th N values show how many cases the correlation was based on

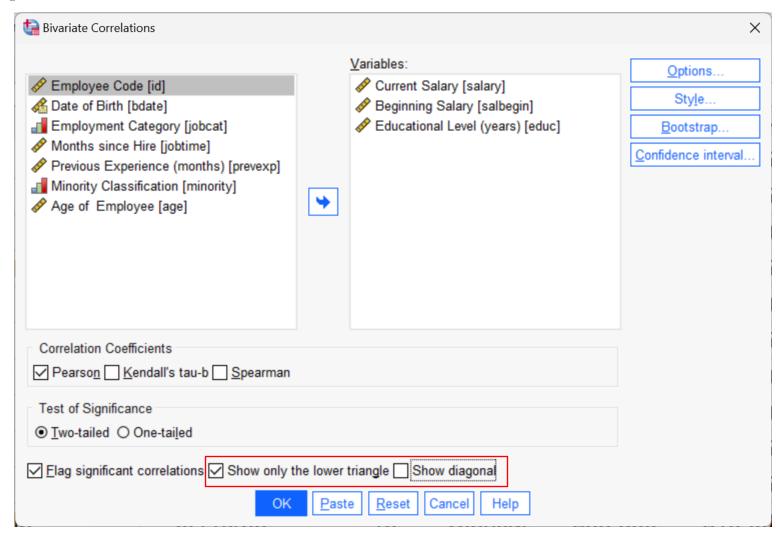
Correlations

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|---------------------------|---------------------|----------------|---------------------|------------------------------|
| Current Salary | Pearson Correlation | 1 | .880** | .661** |
| | Sig. (2-tailed) | | <.001 | <.001 |
| | N | 474 | 474 | 474 |
| Beginning Salary | Pearson Correlation | .880** | 1 | .633** |
| | Sig. (2-tailed) | <.001 | | <.001 |
| | N | 474 | 474 | 474 |
| Educational Level (years) | Pearson Correlation | .661** | .633** | 1 |
| | Sig. (2-tailed) | <.001 | <.001 | |
| | N | 474 | 474 | 474 |

^{**.} Correlation is significant at the 0.01 level (2-tailed).



- We can re-run the analysis, but this time....
 - Show only the bottom half of the matrix
 - Don't show the correlations of each variable against itself





Correlations

| | | Current Salary | Beginning Salary |
|---------------------------|---------------------|----------------|---------------------|
| Beginning Salary | Pearson Correlation | .880** | |
| | Sig. (2-tailed) | <.001 | |
| | N | 474 | |
| Educational Level (years) | Pearson Correlation | .661** | .633** |
| | Sig. (2-tailed) | <.001 | <.001 |
| | N | 474 | 474 |

^{**.} Correlation is significant at the 0.01 level (2-tailed).



Let's explore Pearson's correlations in SPSS Statistics



$$r = rac{\sum \left(x_i - ar{x}
ight)\left(y_i - ar{y}
ight)}{\sqrt{\sum \left(x_i - ar{x}
ight)^2 \sum \left(y_i - ar{y}
ight)^2}}$$

How is a Pearson's correlation calculated?

Pearson's *r* (the most well known correlation measure)

- In statistics, the **Pearson correlation coefficient** is also known as **Pearson's r** or the **Pearson product-moment** correlation coefficient
- Correlations describe data moving together
- This is a **parametric** procedure. That means it makes assumptions about the data. Strictly speaking Pearson's *r* assumes the following:
 - The level of measurement of the variables are continuous/scale (i.e. interval or ratio)
 - There should be no extreme outliers in the correlated variables
 - The data are <u>normally distributed</u> this is not needed for a reasonable sample size



Formula for Pearson's r

$$r = rac{\sum \left(x_i - ar{x}
ight)\left(y_i - ar{y}
ight)}{\sqrt{\sum \left(x_i - ar{x}
ight)^2 \sum \left(y_i - ar{y}
ight)^2}}$$

r = correlation coefficient

 $oldsymbol{x}_i$ = values of the x-variable in a sample

 $ar{x}$ = mean of the values of the x-variable

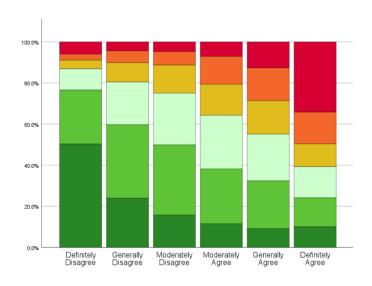
 y_i = values of the y-variable in a sample

 $ar{oldsymbol{y}}$ = mean of the values of the y-variable



Let's see an example of calculating Pearson's R

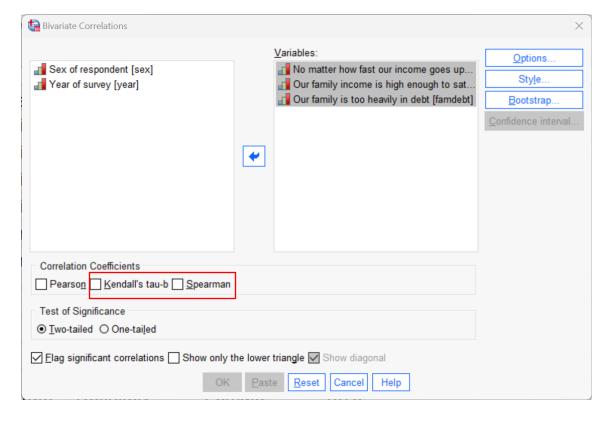




Correlations with rank order variables

Correlations for Ordinal Variables

- Rank order or 'ordinal' variables refer to variables such as rating scales
- These are not true numbers, but rather ranked 'numerals'
- Two techniques exist in SPSS that deal with these kind of data
 - Spearman's Rho
 - Kendall's Tau-b
- Both are non-parametric methods





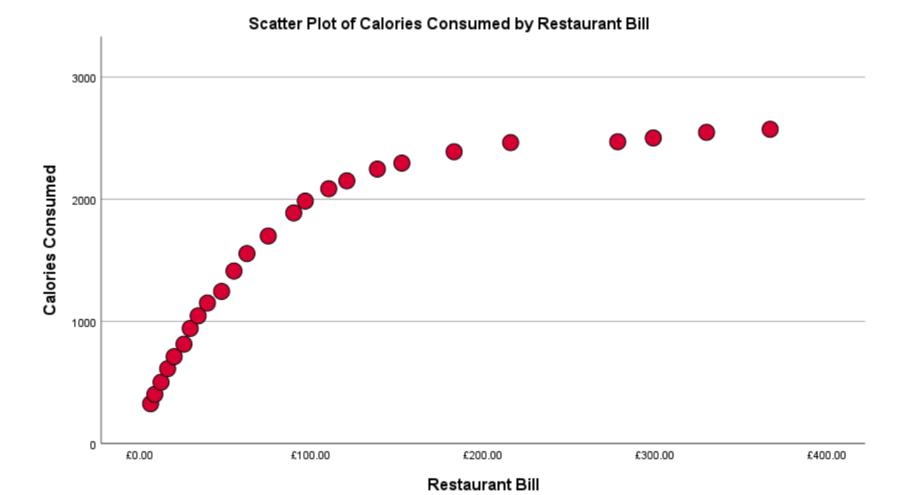
Spearman's Rho

- Spearman's Rho works by ranking the original values from the lowest number to the highest
- For this reason, it's sometimes referred to as Spearman's Rank Correlation
- Spearman's correlation detects *monotonic* relationships. A monotonic relationship is one in which, as the size of one variable increases, the other variables also increases, or where the as the size of one variable increases, as the other variable decreases.
- Spearman correlations are not affected by outliers, but analysts should still consider whether extreme outliers are valid reflections of the population under consideration



Spearman's Rho

Consider this non-linear relationship....





Let's explore how Spearman's correlations work

An alternative to Spearman's Correlation: Kendall's Tau b

Kendall's Tau

- Kendall's Tau b also works by ranking the original values from the lowest number to the highest
- However, this time the analysis focuses on *the degree of concordance and discordance* between two ranked columns of data

| | Movie_Title | | Rotten_ | Tomatoes |
|----|------------------------------------|----|---------|-----------------|
| 1 | Uncorked | 1 | * | 76 |
| 2 | Spenser Confidential | 2 | K | / 31 |
| 3 | The Willoughbys | 3 | ~ | 75 |
| 4 | Tigertail | 4 | R / | >3 |
| 5 | Extraction | 5 | | 2 |
| 6 | The Half of It | 6 | K | 8 |
| 7 | To All the Boys I've Loved Before | 7 | K | 9 |
| 8 | LA Originals | 8 | | 4 |
| 9 | Miss Americana | 9 | | 7 |
| 10 | Crip Camp: A Disability Revolution | 10 | < | → 10 |



Kendall's Tau

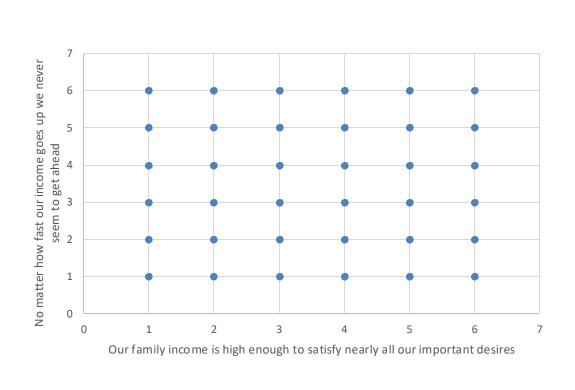
- Some argue that the significance estimates and confidence intervals for Kendall's Tau tend to be more reliable than for Spearman correlations.
- Kendall's Tau tend to give smaller correlation values than Spearman's and can also take much longer to calculate

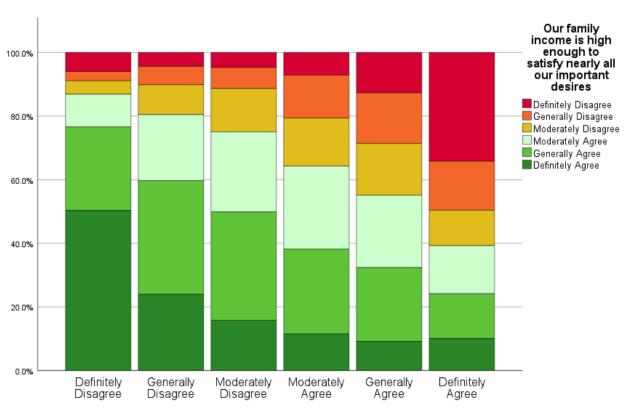
| | Movie_Title | | Rotten_Tomatoes | |
|----|------------------------------------|----|-----------------|---|
| 1 | Uncorked | 1 | 7 | 6 |
| 2 | Spenser Confidential | 2 | K >>> | 1 |
| 3 | The Willoughbys | 3 | * 7 | 5 |
| 4 | Tigertail | 4 | | 3 |
| 5 | Extraction | 5 | 4 | 2 |
| 6 | The Half of It | 6 | K | 8 |
| 7 | To All the Boys I've Loved Before | 7 | * | 9 |
| 8 | LA Originals | 8 | 4 | 4 |
| 9 | Miss Americana | 9 | Y | 7 |
| 10 | Crip Camp: A Disability Revolution | 10 | <> 1□ | 0 |
| | | | | |



Let's compare Kendall's Tau to Spearman's correlations

Visualising Correlations for Ordinal Variables





No matter how fast our income goes up we never seem to get ahead

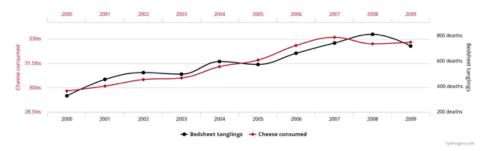


May require a different approach than scatterplots



Per capita cheese consumption

Number of people who died by becoming tangled in their bedsheets



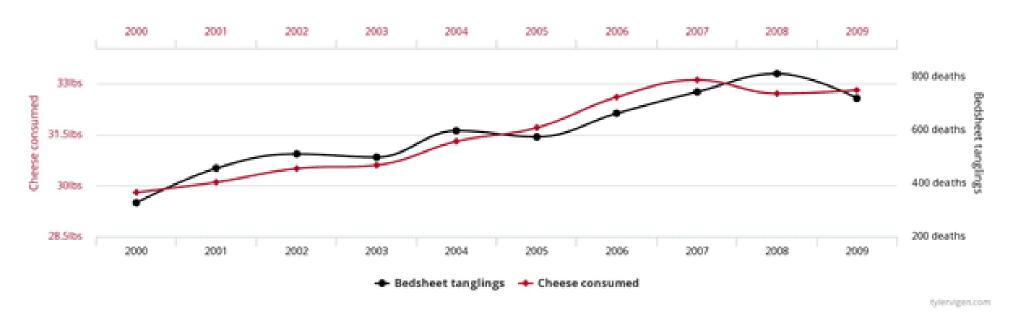
The Limitations of Correlations

Correlation does not indicate causation

Per capita cheese consumption

correlates with

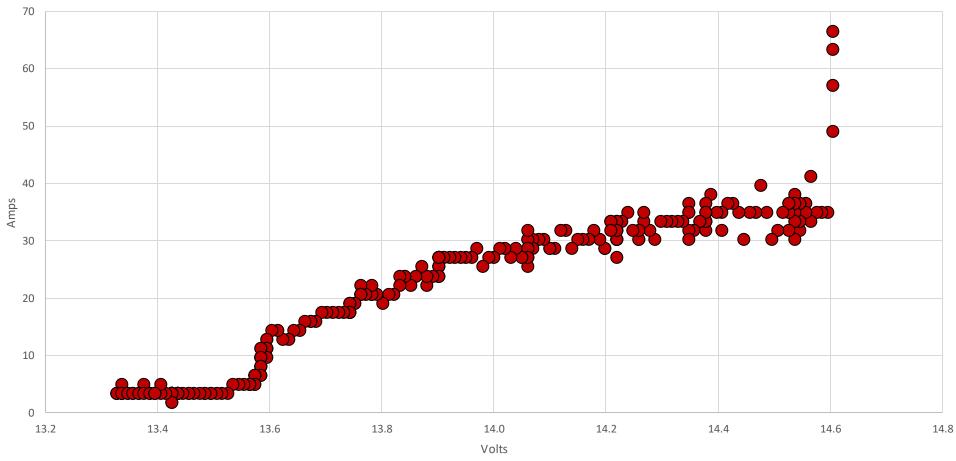
Number of people who died by becoming tangled in their bedsheets



https://www.productleadership.com/does-causation-imply-correlation/



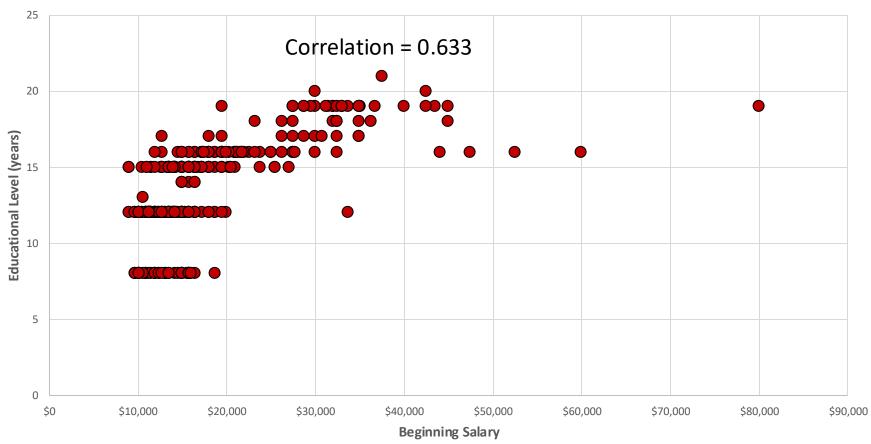
Can't accurately measure curvilinear relationships





Are influenced by the range of values in the sample

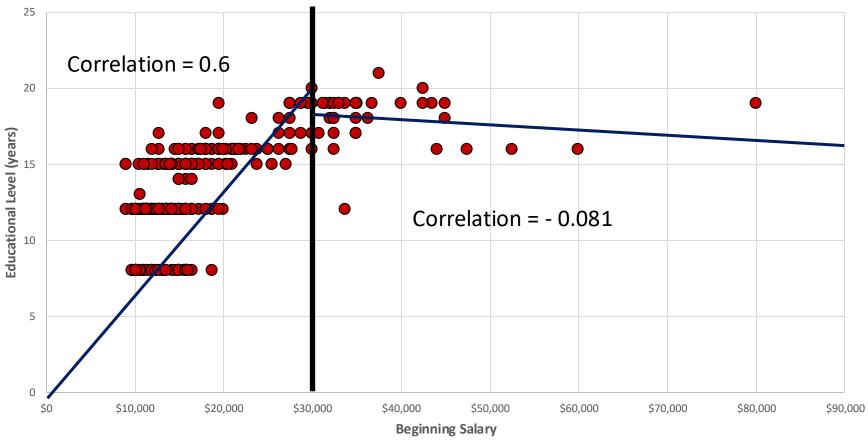






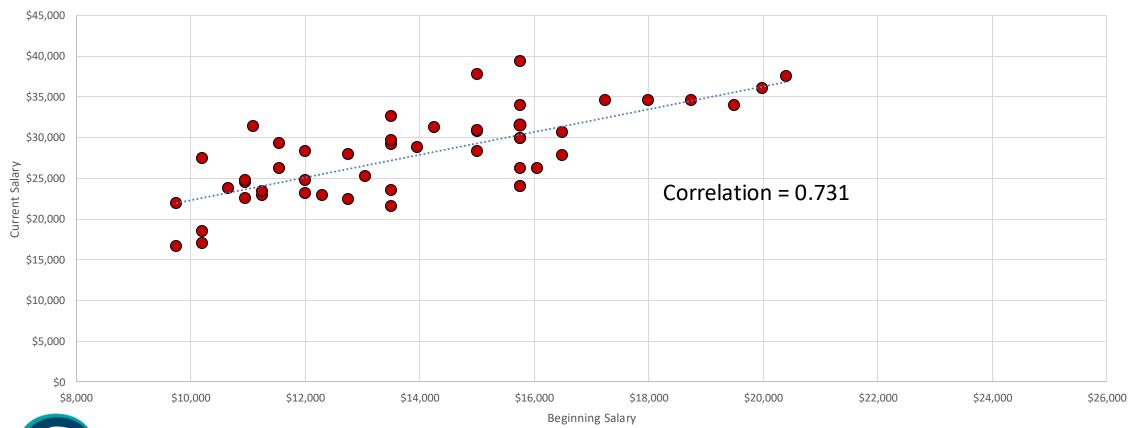
Are influenced by the range of values in the sample





Can be unduly affected by extreme/outlier values

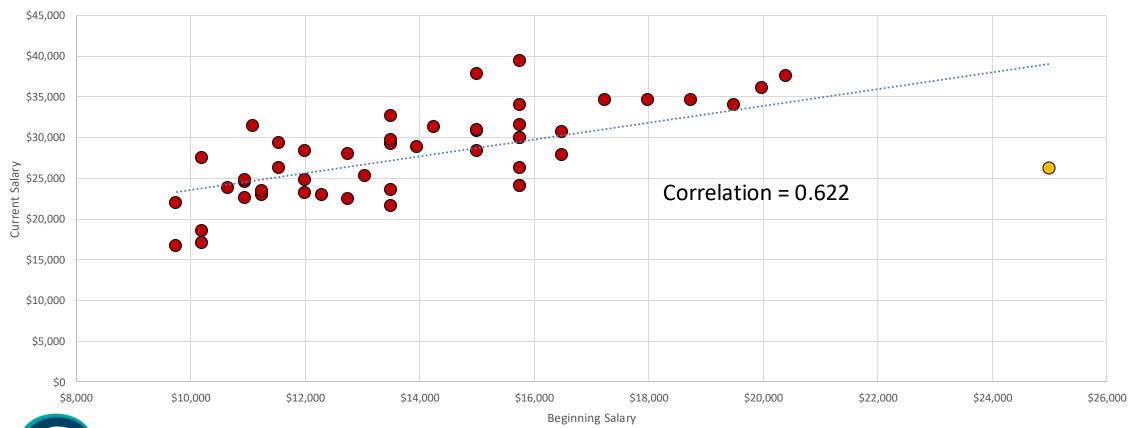






Can be unduly affected by extreme/outlier values







Online training materials free to Smart Vision customers or available for purchase



Factor and Cluster Analysis with IBM SPSS Statistics

£75.00 Jarlath Quinn



Introduction to Time Series Forecasting with IBM SPSS Statistics

£75.00 Jarlath Quinn



Understanding and applying logistic regression techniques in SPSS Statistics

£75.00 Jarlath Quinn



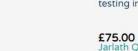
Building predictive models in SPSS Modeler

£75.00

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Statistical and significance testing in SPSS Statistics







Introduction to IBM SPSS Statistics course





Understanding and Applying Linear Regression Techniques in SPSS Statistics

Working with decision trees in SPSS Statistics



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- Delivery of classroom training courses / side by side training support
- Identification & recruitment of analytical skills into your organisation

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